

LECTURE 5

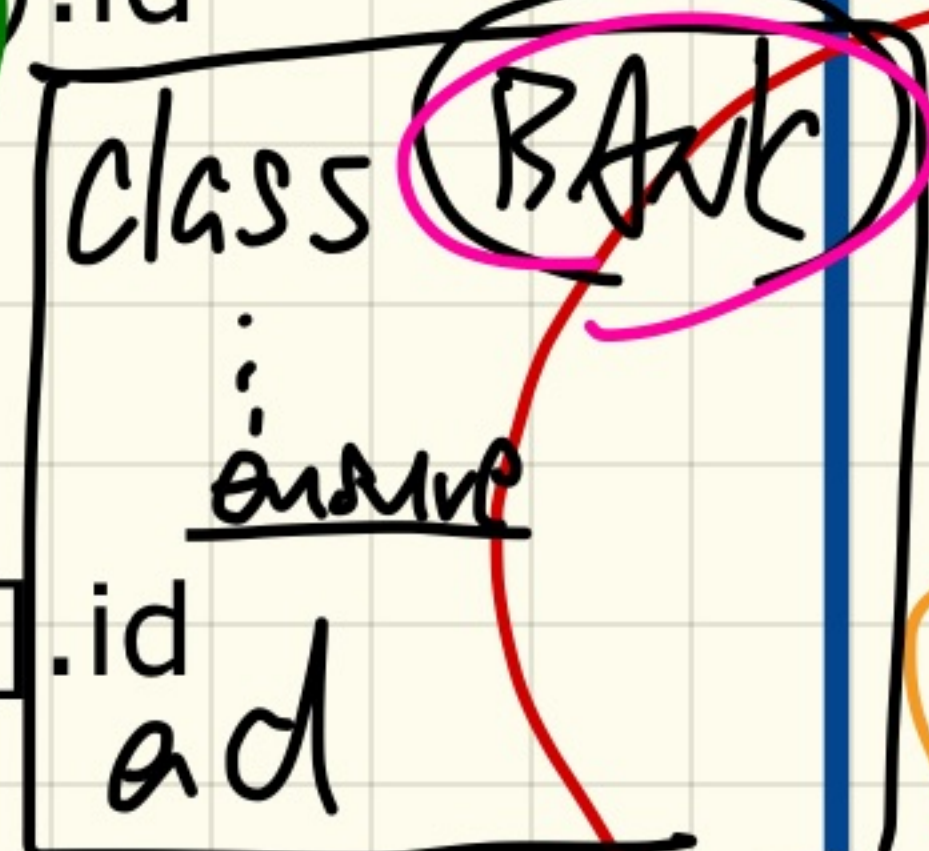
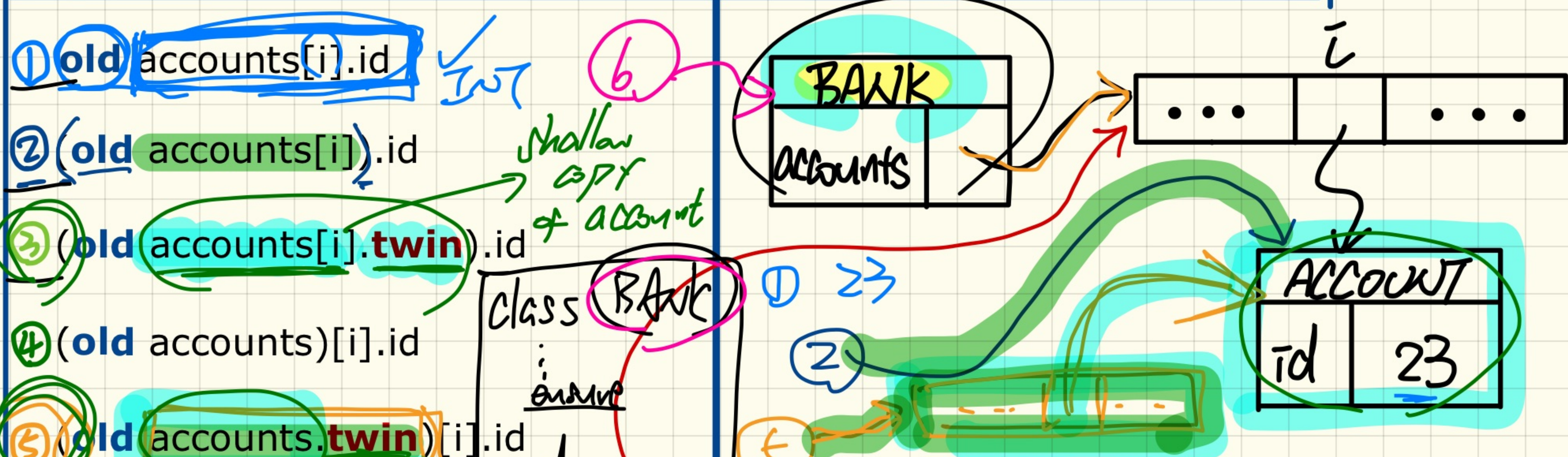
THURSDAY SEPTEMBER 19

Caching Values for **old** Expressions in Postconditions

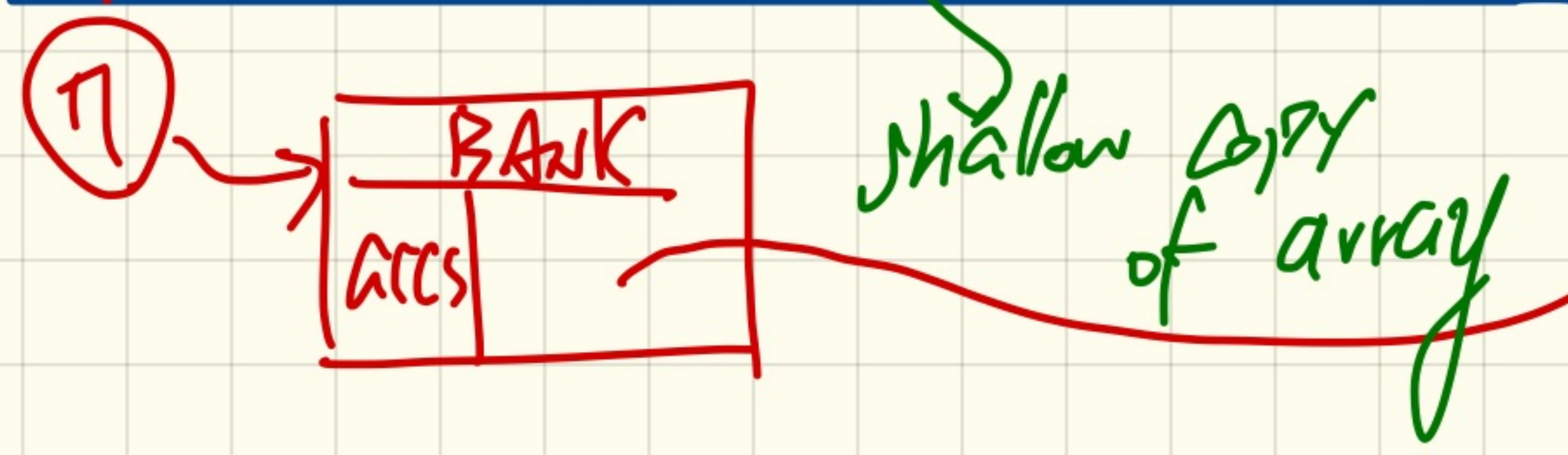
ensure (in context of **BANK**)

- ① **old** accounts[i].id
- ② (**old** accounts[i]).id
- ③ (**old** accounts[i].**twin**).id
- ④ (**old** accounts)[i].id
- ⑤ (**old** accounts.**twin**)[i].id
- ⑥ (**old** **Current**).accounts[i].id
- ⑦ (**old** **Current**.**twin**).accounts[i].id

How to Cache at Runtime?



- ① := accounts[i].id
- ② := accounts[i]
- ⑤ := accounts.twin
- ⑦ := Current.twin
- ⑥ := Current




```

class BANK
create make
feature
  accounts: ARRAY[ACCOUNT]
  make do create accounts.make_empty end
  account_of (n: STRING): ACCOUNT
    require -- the input name exists
      existing: across accounts is acc some acc.owner ~ n end
      -- not (across accounts is acc all acc.owner /~ n end)
    do ... ensure Result.owner ~ n end
  add (n: STRING)
    require -- the input name does not exist
      non_existing: across accounts is acc all acc.owner /~ n end
      -- not (across accounts is acc some acc.owner ~ n end)
    local new_account: ACCOUNT
    do
      create new_account.make (n)
      accounts.force (new_account, accounts.upper + 1)
    end
end
end

```

not(across accounts is acc
 all acc.owner ~ n
 end)

```

class ACCOUNT
inherit
  ANY
  redefine is_equal end
create
  make
feature -- Attributes
  owner: STRING
  balance: INTEGER
feature -- Commands
  make (n: STRING)
  do
    owner := n
    balance := 0
  end

```

```

deposit(a: INTEGER)
do
  balance := balance + a
  ensure
    balance = old balance + a
  end

is_equal(other: ACCOUNT): BOOLEAN
do
  Result :=
    owner ~ other.owner
  and balance = other.balance
end
end

```

$$\forall x: R(x) \cdot P(x) \\
 \equiv \neg(\exists x: R(x) \wedge \neg P(x))$$

f

regular

tag ✓

-To Do

g(...)

Agross

f

EMRP

tag: To do
✓ h(-)

g(-)

h(-)

do

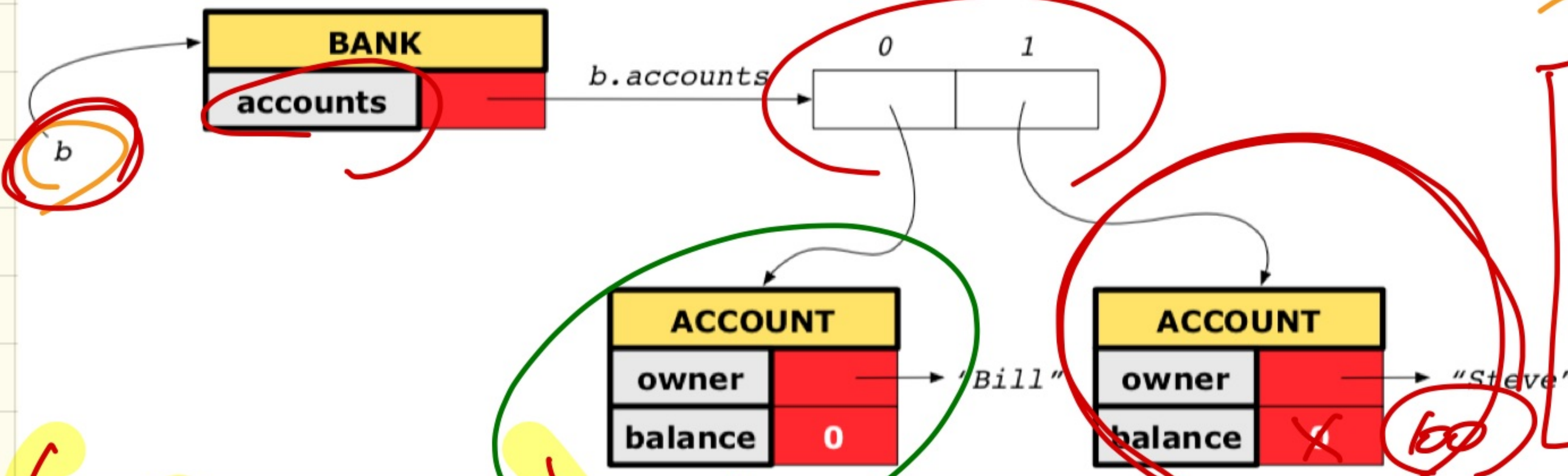
end

Unit Test for All 5 Versions

```
class TEST_BANK
  test_bank_deposit_correct_imp_incomplete_contract: BOOLEAN
  local
    b: BANK
  do
    comment ("t1: correct imp and incomplete contract")
    → create b.make
      b.add ("Bill")
      b.add ("Steve")

      -- deposit 100 dollars to Steve's account
    → b.deposit_on_v1 ("Steve", 100)
      Result :=
        b.account_of("Bill").balance = 0
      and b.account_of("Steve").balance = 100
      check Result end
  end
end
```


Version 1: Incomplete Contracts, Correct Implementation



b.deposit("Steve", 100)

pre-state: 2
 $old_count := accounts.count$
 $old_balance :=$
 $Current.a - 0(n).b$

$(old\ Current.a - 0(n)).balance$

Incomplete
 - it talks
 nothing about
 all other
 accounts.

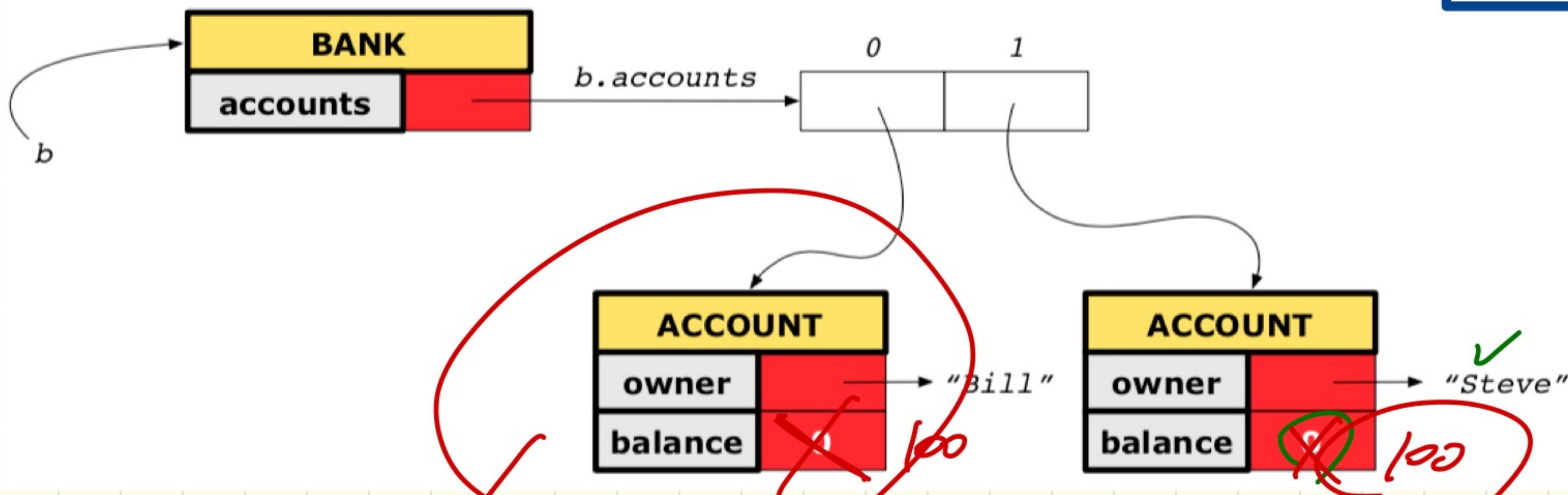
```

class BANK
  deposit_on_v1 (n: STRING; a: INTEGER)
  require across accounts is acc some acc.owner ~ n end
  local i: INTEGER
  do
    from i := accounts.lower
    until i > accounts.upper
    loop
      if accounts[i].owner ~ n then accounts[i].deposit(a) end
      i := i + 1
    end
  ensure
    num_of_accounts_unchanged:
    accounts.count = old accounts.count
    balance_of_n_increased:
    Current.account_of(n).balance =
    old Current.account_of(n).balance + a
  end
end
    
```

T
 T

Version 2: Incomplete Contracts, Wrong Implementation

b.deposit("Steve", 100)



```

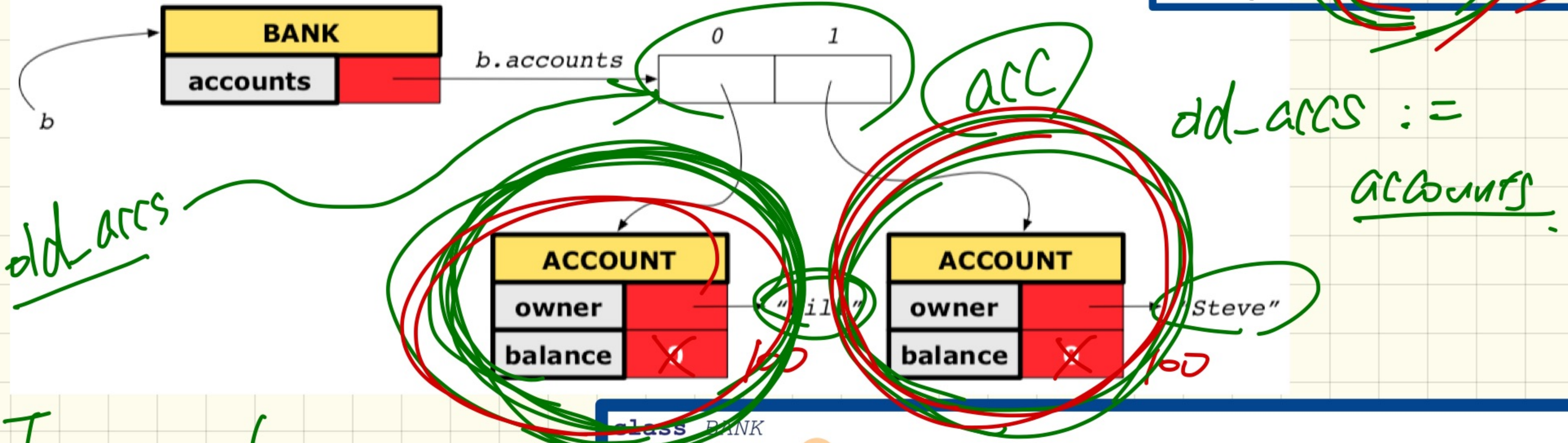
class BANK
  deposit_on_v2 (n: STRING; a: INTEGER)
    require across accounts is acc some acc.owner ~ n end
    local i: INTEGER
    do ...
      -- imp. of version 1, followed by a deposit into 1st account
      → accounts[accounts.lower].deposit(a)
      ensure
        num_of_accounts_unchanged: 2
        accounts.count = old accounts.count
        balance_of_n_increased:
          Current.account_of(n).balance = 0
          old Current.account_of(n).balance + a
      end
    end
end
  
```

how this object (ref of accounts) should be changed and not addressed in postcond.

(T)
(T)
100

Version 3: Complete Contracts (Ref. Copy), Correct Implementation

b.deposit("Steve", 100)



Iteration 1

"Bill" ~ "Steve" implies
 ↳ true simply because we considered the object

Iteration 2
 "Steve" ~ "Steve" implies
 equal to self.

```

class BANK
  deposit_on_v3 (n: STRING; a: INTEGER)
  require across accounts is acc some acc.owner ~ n end
  → local i: INTEGER
  do ...
    [ -- imp. of version 1, followed by a deposit into 1st account
      accounts[accounts.lower].deposit(a) ]
  ensure
    num_of_accounts_unchanged: accounts.count = old accounts.count
    balance_of_n_increased:
      Current.account_of(n).balance =
        old Current.account_of(n).balance + a
    others_unchanged:
      across old accounts is acc
      all
        acc.owner /~ n implies acc ~ Current.account_of(acc.owner)
      end
  end
end
    
```

Handwritten annotations on the code: "2 iterations" with an arrow pointing to the 'across' block, and "Bill" and "Steve" written near the 'acc' variable in the 'all' block.

Use of **across** in **Postcondition**

Version 1

across **old** accounts **is** acc
all

acc.owner /~ n

implies

acc ~ **Current**.account_of (acc.owner)

end

Version 2

across (**old** accounts.lower |..| **old** accounts.upper) **is** i
all

(**old** accounts)[i].owner /~ n

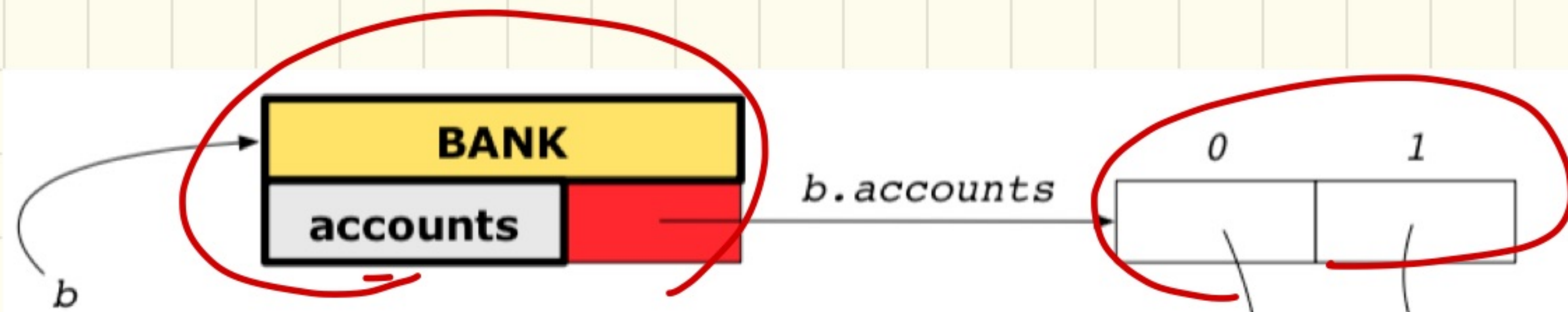
implies

(**old** accounts)[i] ~ **Current**.account_of ((**old** accounts)[i].owner)

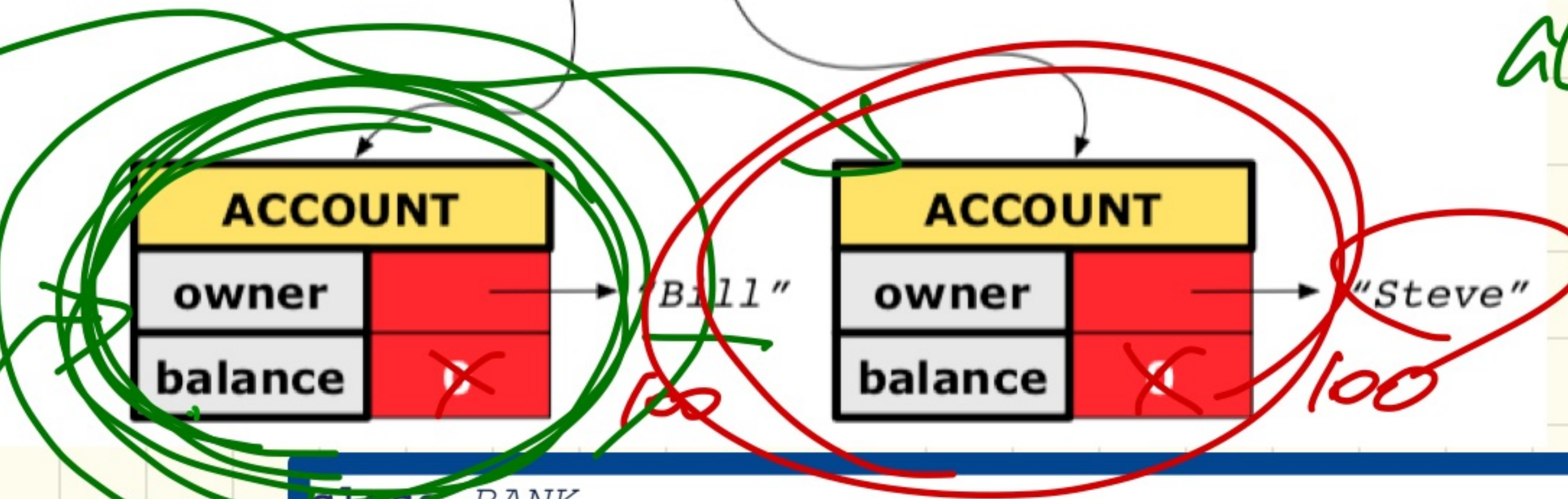
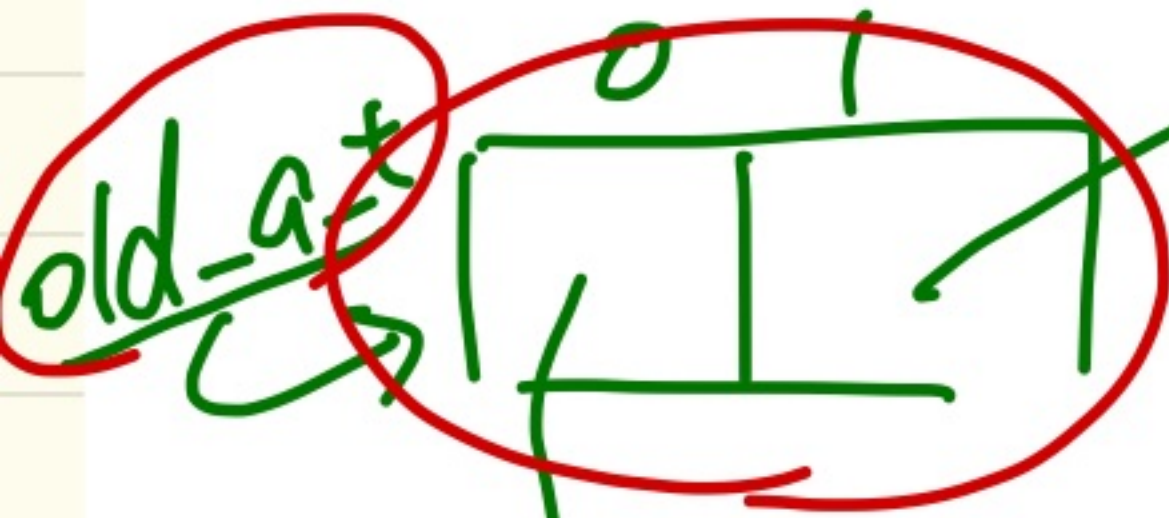
end

Version 4: Complete Contracts (Shallow Copy), Correct Implementation

b.deposit("Steve", 100)



old_a_t :=
accounts.twin



1st iteration

"Bill" /~ "Steve" ⇒

2nd iteration

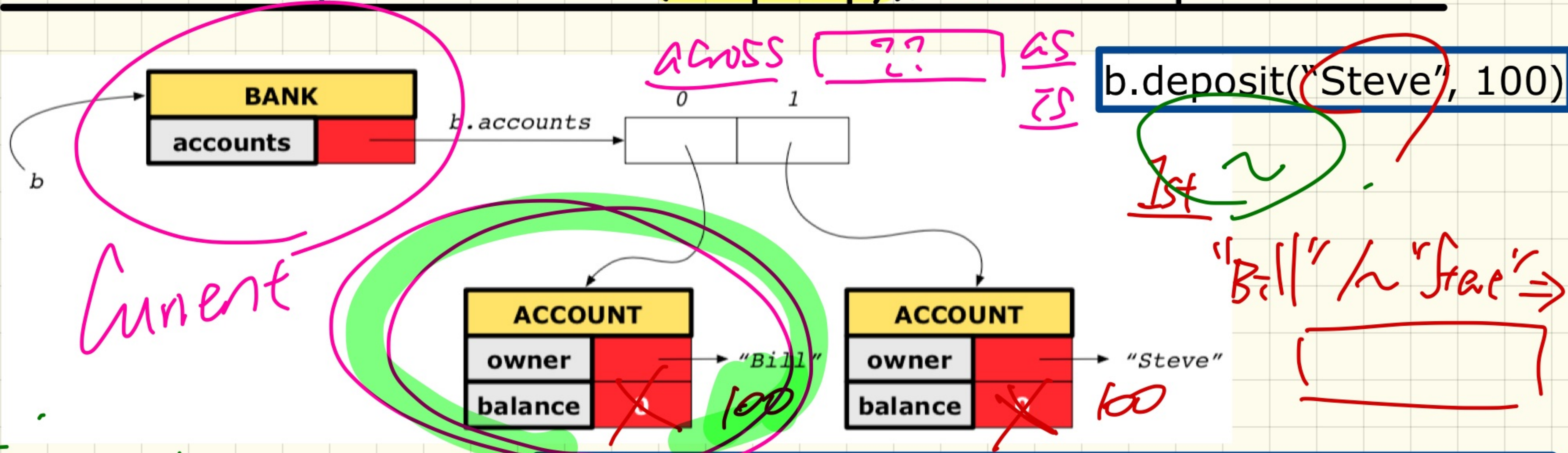
"Steve" /~ "Steve" ⇒

```

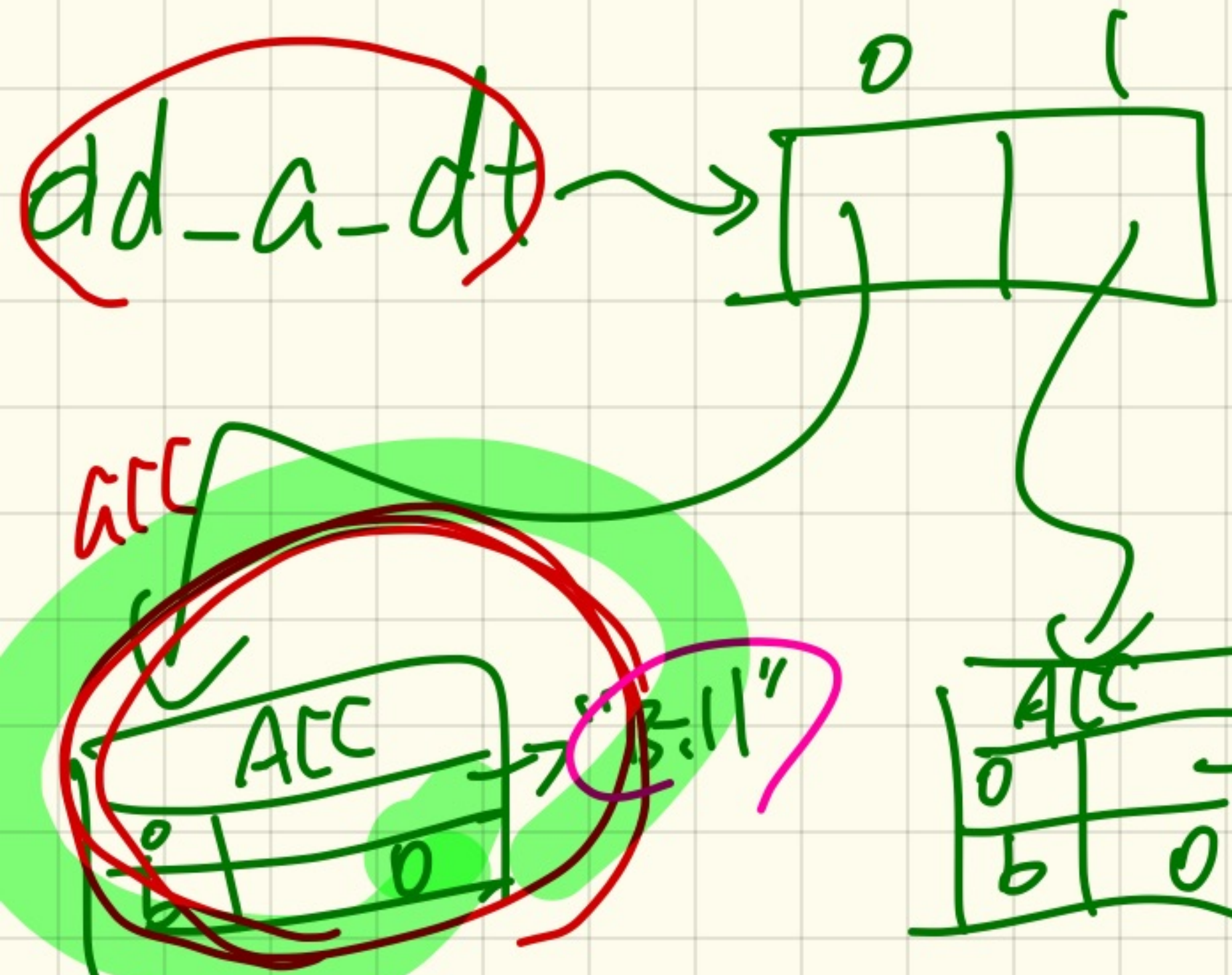
class BANK
  deposit_on_v4 (n: STRING; a: INTEGER)
    require across accounts is acc some acc.owner ~ n end
    local i: INTEGER
    do ...
      -- imp. of version 1, followed by a deposit into 1st account
      accounts[accounts.lower].deposit(a)
      ensure
        num_of_accounts_unchanged: accounts.count = old accounts.count
        balance_of_n_increased:
          Current.account_of(n).balance =
            old Current.account_of(n).balance + a
        others_unchanged:
          across old accounts.twin is acc
          all
            acc.owner /~ n implies acc ~ Current.account_of(acc.owner)
          end
        end
      end
    end
  end
end
  
```

same object

Version 5: Complete Contracts (Deep Copy), Correct Implementation

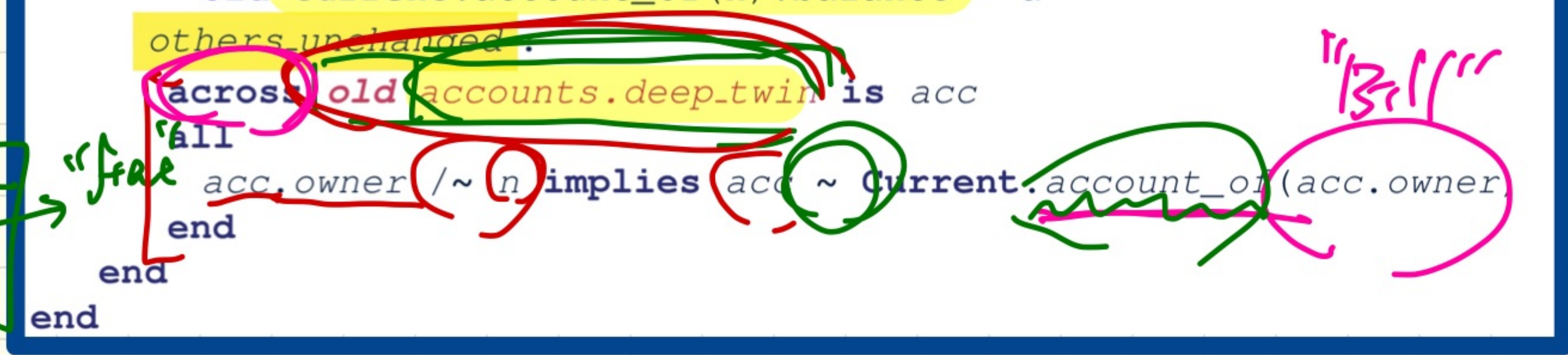


dd_a_dt := accounts.deep_twin



```

class BANK
  deposit_on_v5 (n: STRING; a: INTEGER)
    require across accounts is acc some acc.owner ~ n end
    local i: INTEGER
  do ...
    -- imp. of version 1, followed by a deposit into 1st account
    accounts[accounts.lower].deposit(a)
  ensure
    num_of_accounts_unchanged: accounts.count = old accounts.count
    balance_of_n_increased:
      Current.account_of(n).balance =
        old Current.account_of(n).balance + a
    others_unchanged.
    across old accounts.deep_twin is acc
    all
      acc.owner /~ n implies acc ~ Current.account_of(acc.owner)
    end
  end
end
  
```



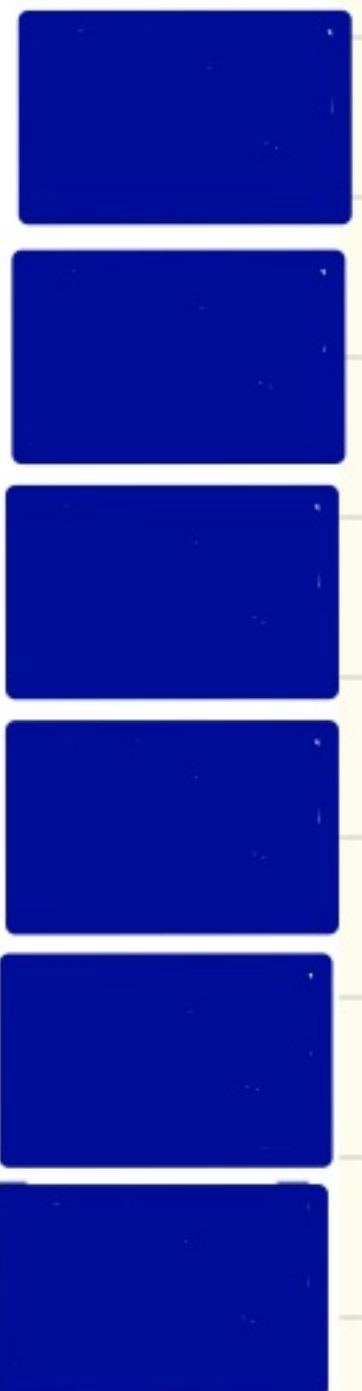
Complete Postcondition: Exercise



Consider the query *account_of* (*n*: *STRING*) of *BANK*.

How do we specify (part of) its postcondition to assert that the state of the bank remains unchanged:

- `accounts = old accounts`
- `accounts = old accounts.twain`
- `accounts = old accounts.deep_twain`
- `accounts ~ old accounts`
- `accounts ~ old accounts.twain`
- `accounts ~ old accounts.deep_twain`



Writing Postcondition: Exercise 1.1

is_positive (i: **INTEGER**): **BOOLEAN**

ensure

i > 0

$\neg \text{is_p}(\exists)$

$\neg \text{is_p}(-4) \leftarrow$

Result correctly
set to false
but a postcond-
violation

Writing Postcondition: Exercise 1.2

```
is_positive (x: INTEGER): BOOLEAN  
  ensure  
    if x > 0 then  
      Result = True  
    end
```

→ Syntax

$x > 0$ implies Result

$\neg (x > 0)$ implies not Result

else
 not Result
end